

# Package ‘matrixdist’

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**Type** Package

**Title** Statistics for Matrix Distributions

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**Maintainer** Martin Bladt <martinbladt@gmail.com>

**Description** Tools for homogeneous and in-homogeneous phase-type distributions.

Methods for functional evaluation, simulation and estimation using the expectation-maximization (EM) algorithm are provided.

The methods of this package are based on the following references.

Asmussen, S., Nerman, O., & Olsson, M. (1996) <<https://www.jstor.org/stable/4616418>>.

Olsson, M. (1996) <<https://www.jstor.org/stable/4616419>>.

Albrecher, H., & Bladt, M. (2019) <[doi:10.1017/jpr.2019.60](https://doi.org/10.1017/jpr.2019.60)>

Albrecher, H., Bladt, M., & Yslas, J. (2020) <[doi:10.1111/sjos.12505](https://doi.org/10.1111/sjos.12505)>

Bladt, M., & Yslas, J. (2020) <[arXiv:2011.03219](https://arxiv.org/abs/2011.03219)>.

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---

matrixdist-package      *Statistics for Matrix Distributions*

---

### Description

This package is concerned with homogeneous and inhomogeneous phase-type distributions. Methods for functional evaluation, simulation and estimation using the EM algorithm are provided.

### Author(s)

Martin Bladt and Jorge Yslas.

Maintainer: Martin Bladt <martinbladt@gmail.com>

### References

Asmussen, S., Nerman, O., & Olsson, M. (1996). Fitting phase-type distributions via the EM algorithm. *Scandinavian Journal of Statistics*, 419-441.

Olsson, M. (1996). Estimation of phase-type distributions from censored data. *Scandinavian journal of statistics*, 443-460.

Albrecher, H., & Bladt, M. (2019). Inhomogeneous phase-type distributions and heavy tails. *Journal of Applied Probability*, 56(4), 1044-1064.

Albrecher, H., Bladt, M., & Yslas, J. (2020). Fitting inhomogeneous Phase-Type distributions to data: The univariate and the multivariate case. *Scandinavian Journal of Statistics*.

Bladt, M., & Yslas, J. (2020). Inhomogeneous Markov Survival Regression Models. arXiv:2011.03219.

---

+ , ph , ph-method      *Sum Method for phase type distributions*

---

### Description

Sum Method for phase type distributions

### Usage

```
## S4 method for signature 'ph,ph'  
e1 + e2
```

### Arguments

e1                    an object of class `ph`.

e2                    an object of class `ph`.

### Value

An object of class `ph`.

**Examples**

```
ph1 <- ph(structure = "general", dimension = 3)
ph2 <- ph(structure = "gcoxian", dimension = 5)
ph_sum <- ph1 + ph2
ph_sum
```

---

a\_rungekutta

*Runge Kutta for the calculation of the a vectors in a EM step*


---

**Description**

Can be used for the loglikelihood

**Usage**

```
a_rungekutta(avector, dt, h, S)
```

**Arguments**

avector	the a vector
dt	increment
h	step-length
S	sub-intensity

---

cdf

*New Generic for the Distribution of Matrix Distributions*


---

**Description**

Methods are available for objects of class [ph](#)

**Usage**

```
cdf(x, ...)
```

**Arguments**

x	an object of the model class.
...	further parameters to be passed on

**Value**

CDF from the matrix distribution.

---

cdf,iph-method	<i>Distribution Method for inhomogeneous phase type distributions</i>
----------------	---

---

**Description**

Distribution Method for inhomogeneous phase type distributions

**Usage**

```
## S4 method for signature 'iph'  
cdf(x, q, lower.tail = TRUE)
```

**Arguments**

x	an object of class <a href="#">iph</a> .
q	a vector of locations.
lower.tail	logical parameter specifying whether lower tail (cdf) or upper tail is computed.

**Value**

A list containing the locations and corresponding CDF evaluations.

**Examples**

```
obj <- iph(ph(structure = "general"), gfun = "weibull", gfun_pars = 2)  
cdf(obj, c(1, 2, 3))
```

---

cdf,ph-method	<i>Distribution Method for phase type distributions</i>
---------------	---

---

**Description**

Distribution Method for phase type distributions

**Usage**

```
## S4 method for signature 'ph'  
cdf(x, q, lower.tail = TRUE)
```

**Arguments**

x	an object of class <a href="#">ph</a> .
q	a vector of locations.
lower.tail	logical parameter specifying whether lower tail (cdf) or upper tail is computed.

**Value**

A list containing the locations and corresponding CDF evaluations.

**Examples**

```
obj <- ph(structure = "general")
cdf(obj, c(1, 2, 3))
```

---

clone_matrix	<i>Clone a matrix</i>
--------------	-----------------------

---

**Description**

Clone a matrix

**Usage**

```
clone_matrix(m)
```

**Arguments**

m                    a matrix

---

clone_vector	<i>Clone a vector</i>
--------------	-----------------------

---

**Description**

Clone a vector

**Usage**

```
clone_vector(v)
```

**Arguments**

v                    a vector



---

coef,iph-method	<i>Coef Method for iph Class</i>
-----------------	----------------------------------

---

**Description**

Coef Method for iph Class

**Usage**

```
## S4 method for signature 'iph'  
coef(object)
```

**Arguments**

object            an object of class [iph](#).

**Value**

parameters of iph model.

**Examples**

```
obj <- iph(ph(structure = "general", dimension = 2), gfun = "lognormal", gfun_pars = 2)  
coef(obj)
```

---

coef,ph-method	<i>Coef Method for ph Class</i>
----------------	---------------------------------

---

**Description**

Coef Method for ph Class

**Usage**

```
## S4 method for signature 'ph'  
coef(object)
```

**Arguments**

object            an object of class [ph](#).

**Value**

Parameters of ph model.

**Examples**

```
obj <- ph(structure = "general")  
coef(obj)
```

coef, sph-method      *Coef Method for sph Class*

---

**Description**

Coef Method for sph Class

**Usage**

```
## S4 method for signature 'sph'  
coef(object)
```

**Arguments**

object      an object of class [sph](#).

**Value**

parameters of sph model

---

cumulateMatrix      *Cumulate matrix*

---

**Description**

Creates a new matrix with entries the cumulated rows of A

**Usage**

```
cumulateMatrix(A)
```

**Arguments**

A      A matrix

**Value**

The cumulated matrix

---

cumulateVector	<i>Cumulate vector</i>
----------------	------------------------

---

**Description**

Creates a new vector with entries the cumulated entries of A

**Usage**

```
cumulateVector(A)
```

**Arguments**

A	A vector
---	----------

**Value**

The cumulated vector

---

default_step_length	<i>Default size of the steps in the RK</i>
---------------------	--

---

**Description**

Computes the default step length for a matrix S to be employed in the RK method

**Usage**

```
default_step_length(S)
```

**Arguments**

S	sub-intensity matrix
---	----------------------

**Value**

The step length for S

---

dens *New Generic for the Density of Matrix Distributions*

---

**Description**

Methods are available for objects of class `ph`

**Usage**

```
dens(x, ...)
```

**Arguments**

`x` an object of the model class.  
`...` further parameters to be passed on

**Value**

Density from the matrix distribution.

---

dens,iph-method *Density Method for inhomogeneous phase type distributions*

---

**Description**

Density Method for inhomogeneous phase type distributions

**Usage**

```
## S4 method for signature 'iph'  
dens(x, y)
```

**Arguments**

`x` an object of class `iph`.  
`y` a vector of locations.

**Value**

A list containing the locations and corresponding density evaluations.

**Examples**

```
obj <- iph(ph(structure = "general"), gfun = "weibull", gfun_pars = 2)  
dens(obj, c(1, 2, 3))
```

---

dens,ph-method	<i>Density Method for phase type distributions</i>
----------------	--

---

**Description**

Density Method for phase type distributions

**Usage**

```
## S4 method for signature 'ph'  
dens(x, y)
```

**Arguments**

x	an object of class <a href="#">ph</a> .
y	a vector of locations.

**Value**

A list containing the locations and corresponding density evaluations.

**Examples**

```
obj <- ph(structure = "general")  
dens(obj, c(1, 2, 3))
```

---

derivativeMatrixweibull	<i>Derivative of matrix Weibull</i>
-------------------------	-------------------------------------

---

**Description**

Can be used to increase performance

**Usage**

```
derivativeMatrixweibull(h, obs, weight, rcens, rcweight, alpha, S, beta)
```

**Arguments**

h	step-length
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation

---

diagonal_vector	<i>Creates a matrix with the given vector in the diagonal</i>
-----------------	---

---

**Description**

Creates a matrix with the given vector in the diagonal

**Usage**

```
diagonal_vector(vec)
```

**Arguments**

vec	a vector
-----	----------

---

embeddedMC	<i>Embedded Markov chain of a sub-intensity matrix</i>
------------	--

---

**Description**

Returns the transition probabilities of the embedded Markov chain determined the sub-intensity matrix

**Usage**

```
embeddedMC(S)
```

**Arguments**

S	A sub-intensity matrix
---	------------------------

**Value**

The embedded Markov chain

---

EMstep_PADE	<i>EM using Matlab algorithm for matrix exponential in combination with Armadillo</i>
-------------	---

---

**Description**

EM using Matlab algorithm for matrix exponential in combination with Armadillo

**Usage**

EMstep\_PADE(h, alpha, S, obs, weight, rcens, rcweight)

**Arguments**

h	nuisance parameter
alpha	initial probabilities
S	sub-intensity
obs	the observations
weight	the weights for the observations
rcens	censored observations
rcweight	the weights for the censored observations

---

EMstep_RK	<i>EM step using Runge Kutta</i>
-----------	----------------------------------

---

**Description**

Computes one step of the EM algorithm by using a Runge-Kutta method of 4th order

**Usage**

EMstep\_RK(h, alpha, S, obs, weight, rcens, rcweight)

**Arguments**

h	step-length
alpha	initial probabilities
S	sub-intensity
obs	the observations
weight	the weights for the observations
rcens	censored observations
rcweight	the weights for the censored observations

---

EMstep_UNI	<i>EM using Uniformization for matrix exponential</i>
------------	---

---

**Description**

EM using Uniformization for matrix exponential

**Usage**

```
EMstep_UNI(h, alpha, S, obs, weight, rcens, rcweight)
```

**Arguments**

h	positive parameter
alpha	initial probabilities
S	sub-intensity
obs	the observations
weight	the weights for the observations
rcens	censored observations
rcweight	the weights for the censored observations

---

evaluate	<i>New Generic for Evaluating Survival Matrix Distributions</i>
----------	---

---

**Description**

Methods are available for objects of class [sph](#)

**Usage**

```
evaluate(x, subject, ...)
```

**Arguments**

x	an object of the model class.
subject	a vector of data.
...	further parameters to be passed on



---

evaluate, sph-method     *Evaluation Method for sph Class*

---

**Description**

Evaluation Method for sph Class

**Usage**

```
## S4 method for signature 'sph'
evaluate(x, subject)
```

**Arguments**

x	an object of class <a href="#">sph</a> .
subject	covariates of a single subject.

**Value**

a [ph](#) model

---

Fisher	<i>New Generic for obtaining the Fisher Information of Survival Matrix Distributions</i>
--------	--

---

**Description**

Methods are available for objects of class [sph](#)

**Usage**

```
Fisher(x, ...)
```

**Arguments**

x	an object of the model class.
...	further parameters to be passed on

---

Fisher, sph-method	<i>Fisher Information Method for sph Class</i>
--------------------	--

---

**Description**

Fisher Information Method for sph Class

**Usage**

```
## S4 method for signature 'sph'
Fisher(x, y, X, w = numeric(0))
```

**Arguments**

x	an object of class <a href="#">sph</a> .
y	independent variate.
X	matrix of covariates.
w	weights.

**Value**

a matrix.

---

fit	<i>New Generic for Estimating Matrix Distributions</i>
-----	--

---

**Description**

Methods are available for objects of class [ph](#)

**Usage**

```
fit(x, y, ...)
```

**Arguments**

x	an object of the model class.
y	a vector of data.
...	further parameters to be passed on

**Value**

An object of the fitted model class.

---

fit,ph-method

*Fit Method for ph Class*


---

**Description**

Fit Method for ph Class

**Usage**

```
## S4 method for signature 'ph'
fit(
  x,
  y,
  weight = numeric(0),
  rcen = numeric(0),
  rcenweight = numeric(0),
  stepsEM = 1000,
  methods = c("RK", "RK"),
  rkstep = NA,
  uni_epsilon = NA,
  maxit = 100,
  reltol = 1e-08,
  every = 100,
  plot = FALSE
)
```

**Arguments**

x	an object of class <a href="#">ph</a> .
y	vector or data.
weight	vector of weights.
rcen	vector of right-censored observations
rcenweight	vector of weights for right-censored observations.
stepsEM	number of EM steps to be performed.
methods	methods to use for matrix exponential calculation: RM, UNI or PADE
rkstep	Runge-Kutta step size (optional)
uni_epsilon	epsilon parameter for uniformization method
maxit	maximum number of iterations when optimizing g function.
reltol	relative tolerance when optimizing g function.
every	number of iterations between likelihood display updates.
plot	logical indicating whether to plot the fit at each iteration.

**Value**

An object of class `ph`.

**Examples**

```
obj <- iph(ph(structure = "general", dimension = 2), gfun = "weibull", gfun_pars = 2)
data <- sim(obj, n = 100)
fit(obj, data, stepsEM = 1000, every = 200)
```

---

haz

*New Generic for the Hazard rate of Matrix Distributions*


---

**Description**

Methods are available for objects of class `ph`

**Usage**

```
haz(x, ...)
```

**Arguments**

`x` an object of the model class.  
`...` further parameters to be passed on

**Value**

Hazard rate from the matrix distribution.

---

haz,ph-method

*Hazard rate Method for phase type distributions*


---

**Description**

Hazard rate Method for phase type distributions

**Usage**

```
## S4 method for signature 'ph'
haz(x, y)
```

**Arguments**

`x` an object of class `ph`.  
`y` a vector of locations.

**Value**

A list containing the locations and corresponding hazard rate evaluations.

**Examples**

```
obj <- ph(structure = "general")
haz(obj, c(1, 2, 3))
```

---

initialState	<i>Initial state of Markov jump process</i>
--------------	---

---

**Description**

Given the accumulated values of the initial probabilities  $P_i$  and a uniform value  $u$ , it returns the initial state of a Markov jump process

**Usage**

```
initialState(cumulatedPi, u)
```

**Arguments**

cumulatedPi	A vector
u	A random value in (0,1)

**Value**

The initial state of the Markov jump process

---

iph	<i>Constructor Function for inhomogeneous phase type distributions</i>
-----	--

---

**Description**

Constructor Function for inhomogeneous phase type distributions

**Usage**

```
iph(
  ph = NULL,
  gfun = NULL,
  gfun_pars = NULL,
  alpha = NULL,
  S = NULL,
  structure = NULL,
  dimension = 3,
  scale = 1
)
```

**Arguments**

ph	An object of class <a href="#">ph</a> .
gfun	inhomogeneity transform
gfun_pars	the parameters of the inhomogeneity function
alpha	a probability vector.
S	a sub-intensity matrix.
structure	a valid ph structure
dimension	the dimension of the ph structure (if provided)
scale	scale

**Value**

An object of class [iph](#).

**Examples**

```
iph(ph(structure = "coxian", dimension = 4), gfun = "pareto", gfun_pars = 3)
```

---

 iph-class

---

*Inhomogeneous Phase Type distributions*


---

**Description**

Class of objects for inhomogeneous phase type distributions

**Value**

Class object

**Slots**

name name of the phase type distribution.

gfun a list comprising of the parameters.

scale scale.

---

LInf_norm	<i>L-oo norm of a matrix</i>
-----------	------------------------------

---

**Description**

Computes the L-oo norm of a matrix A, which is defined as:  $L\text{-oo } A = \max ( 1 \leq I \leq M ) \sum ( 1 \leq J \leq N ) \text{abs} ( A(I,J) )$ .

**Usage**

```
LInf_norm(A)
```

**Arguments**

A	A matrix
---	----------

---

logLik,ph-method	<i>logLik Method for ph Class</i>
------------------	-----------------------------------

---

**Description**

logLik Method for ph Class

**Usage**

```
## S4 method for signature 'ph'
logLik(object)
```

**Arguments**

object	an object of class <a href="#">ph</a> .
--------	---

**Value**

An object of class logLik.

**Examples**

```
obj <- iph(ph(structure = "general", dimension = 2), gfun = "weibull", gfun_pars = 2)
data <- sim(obj, n = 100)
fitted_ph <- fit(obj, data, stepsEM = 10)
logLik(fitted_ph)
```

---

logLikelihoodMgev\_PADE

*Loglikelihood of matrix-GEV using Pade*

---

### Description

Loglikelihood for a sample

### Usage

logLikelihoodMgev\_PADE(h, alpha, S, beta, obs, weight, rcens, rcweight)

### Arguments

h	nuisance parameter
alpha	initial probabilities
S	sub-intensity
beta	in-homogeneity parameter
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

logLikelihoodMgev\_RK *Loglikelihood of matrix GEV using RK*

---

### Description

Loglikelihood for a sample

### Usage

logLikelihoodMgev\_RK(h, alpha, S, beta, obs, weight, rcens, rcweight)

### Arguments

h	step-length
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations



---

logLikelihoodMgev\_UNI *Loglikelihood of matrix-GEV using Uniformization*

---

**Description**

Loglikelihood for a sample

**Usage**

logLikelihoodMgev\_UNI(h, alpha, S, beta, obs, weight, rcens, rcweight)

**Arguments**

h	positive parameter
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

logLikelihoodMgompertz\_PADE

*Loglikelihood of matrix-Gompertz using Pade*

---

**Description**

Loglikelihood for a sample

**Usage**

logLikelihoodMgompertz\_PADE(h, alpha, S, beta, obs, weight, rcens, rcweight)

**Arguments**

h	nuisance parameter
alpha	initial probabilities
S	sub-intensity
beta	in-homogeneity parameter
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

`logLikelihoodMgompertz_PADEs`*Loglikelihood of matrix-Gompertz using Pade*

---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMgompertz_PADEs(  
  h,  
  alpha,  
  S,  
  beta,  
  obs,  
  weight,  
  rcens,  
  rcweight,  
  scale1,  
  scale2  
)
```

**Arguments**

<code>h</code>	nuisance parameter
<code>alpha</code>	initial probabilities
<code>S</code>	sub-intensity
<code>beta</code>	in-homogeneity parameter
<code>obs</code>	the observations
<code>weight</code>	weight of the observations
<code>rcens</code>	censored observations
<code>rcweight</code>	weight of the censored observations
<code>scale1</code>	scale for observations
<code>scale2</code>	scale for censored observations

---

 logLikelihoodMgompertz\_RK

*Loglikelihood of matrix Gompertz using RK*


---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMgompertz_RK(h, alpha, S, beta, obs, weight, rcens, rcweight)
```

**Arguments**

h	step-length
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

 logLikelihoodMgompertz\_RKs

*Loglikelihood of matrix-Gompertz using RK*


---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMgompertz_RKs(
  h,
  alpha,
  S,
  beta,
  obs,
  weight,
  rcens,
  rcweight,
  scale1,
  scale2
)
```

**Arguments**

h	positive parameter
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations
scale1	scale for observations
scale2	scale for censored observations

---

logLikelihoodMgompertz\_UNI

*Loglikelihood of matrix-Gompertz using Uniformization*

---

**Description**

Loglikelihood for a sample

**Usage**

logLikelihoodMgompertz\_UNI(h, alpha, S, beta, obs, weight, rcens, rcweight)

**Arguments**

h	positive parameter
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

`logLikelihoodMgompertz_UNIs`*Loglikelihood of matrix-Gompertz using Uniformization*

---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMgompertz_UNIs(  
  h,  
  alpha,  
  S,  
  beta,  
  obs,  
  weight,  
  rcens,  
  rcweight,  
  scale1,  
  scale2  
)
```

**Arguments**

<code>h</code>	positive parameter
<code>alpha</code>	initial probabilities
<code>S</code>	sub-intensity
<code>beta</code>	parameter of transformation
<code>obs</code>	the observations
<code>weight</code>	weight of the observations
<code>rcens</code>	censored observations
<code>rcweight</code>	weight of the censored observations
<code>scale1</code>	scale for observations
<code>scale2</code>	scale for censored observations

---

```
logLikelihoodMloglogistic_PADE
```

*Loglikelihood of matrix-loglogistic using Pade*

---

### Description

Loglikelihood for a sample

### Usage

```
logLikelihoodMloglogistic_PADE(h, alpha, S, beta, obs, weight, rcens, rcweight)
```

### Arguments

h	nuisance parameter
alpha	initial probabilities
S	sub-intensity
beta	in-homogeneity parameter
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

```
logLikelihoodMloglogistic_PADEs
```

*Loglikelihood of matrix-loglogistic using Pade*

---

### Description

Loglikelihood for a sample

### Usage

```
logLikelihoodMloglogistic_PADEs(
  h,
  alpha,
  S,
  beta,
  obs,
  weight,
  rcens,
  rcweight,
  scale1,
  scale2
)
```

**Arguments**

h	nuisance parameter
alpha	initial probabilities
S	sub-intensity
beta	in-homogeneity parameter
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations
scale1	scale for observations
scale2	scale for censored observations

---

logLikelihoodMloglogistic\_RK

*Loglikelihood of matrix Log-Logistic using RK*

---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMloglogistic_RK(h, alpha, S, beta, obs, weight, rcens, rcweight)
```

**Arguments**

h	step-length
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

`logLikelihoodMloglogistic_RKs`*Loglikelihood of matrix-loglogistic using RK*

---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMloglogistic_RKs(  
  h,  
  alpha,  
  S,  
  beta,  
  obs,  
  weight,  
  rcens,  
  rcweight,  
  scale1,  
  scale2  
)
```

**Arguments**

<code>h</code>	positive parameter
<code>alpha</code>	initial probabilities
<code>S</code>	sub-intensity
<code>beta</code>	parameter of transformation
<code>obs</code>	the observations
<code>weight</code>	weight of the observations
<code>rcens</code>	censored observations
<code>rcweight</code>	weight of the censored observations
<code>scale1</code>	scale for observations
<code>scale2</code>	scale for censored observations



---

 logLikelihoodMloglogistic\_UNI

*Loglikelihood of matrix-loglogistic using Uniformization*


---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMloglogistic_UNI(h, alpha, S, beta, obs, weight, rcens, rcweight)
```

**Arguments**

h	positive parameter
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

 logLikelihoodMloglogistic\_UNIs

*Loglikelihood of matrix-loglogistic using Uniformization*


---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMloglogistic_UNIs(
  h,
  alpha,
  S,
  beta,
  obs,
  weight,
  rcens,
  rcweight,
  scale1,
  scale2
)
```

**Arguments**

h	positive parameter
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations
scale1	scale for observations
scale2	scale for censored observations

---

logLikelihoodMlognormal\_PADE

*Loglikelihood of matrix-lognormal using Pade*

---

**Description**

Loglikelihood for a sample

**Usage**

logLikelihoodMlognormal\_PADE(h, alpha, S, beta, obs, weight, rcens, rcweight)

**Arguments**

h	nuisance parameter
alpha	initial probabilities
S	sub-intensity
beta	in-homogeneity parameter
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

`logLikelihoodMlognormal_PADEs`*Loglikelihood of matrix-lognormal using Pade*

---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMlognormal_PADEs(  
  h,  
  alpha,  
  S,  
  beta,  
  obs,  
  weight,  
  rcens,  
  rcweight,  
  scale1,  
  scale2  
)
```

**Arguments**

<code>h</code>	nuisance parameter
<code>alpha</code>	initial probabilities
<code>S</code>	sub-intensity
<code>beta</code>	in-homogeneity parameter
<code>obs</code>	the observations
<code>weight</code>	weight of the observations
<code>rcens</code>	censored observations
<code>rcweight</code>	weight of the censored observations
<code>scale1</code>	scale for observations
<code>scale2</code>	scale for censored observations

---

logLikelihoodMlognormal\_RK

*Loglikelihood of matrix LogNormal using RK*

---

### Description

Loglikelihood for a sample

### Usage

```
logLikelihoodMlognormal_RK(h, alpha, S, beta, obs, weight, rcens, rcweight)
```

### Arguments

h	step-length
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

logLikelihoodMlognormal\_RKs

*Loglikelihood of matrix-lognormal using RK*

---

### Description

Loglikelihood for a sample

### Usage

```
logLikelihoodMlognormal_RKs(
  h,
  alpha,
  S,
  beta,
  obs,
  weight,
  rcens,
  rcweight,
  scale1,
  scale2
)
```

**Arguments**

h	positive parameter
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations
scale1	scale for observations
scale2	scale for censored observations

---

logLikelihoodMlognormal\_UNI

*Loglikelihood of matrix-lognormal using Uniformization*

---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMlognormal_UNI(h, alpha, S, beta, obs, weight, rcens, rcweight)
```

**Arguments**

h	positive parameter
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

`logLikelihoodMlognormal_UNIs`*Loglikelihood of matrix-lognormal using Uniformization*

---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMlognormal_UNIs(  
  h,  
  alpha,  
  S,  
  beta,  
  obs,  
  weight,  
  rcens,  
  rcweight,  
  scale1,  
  scale2  
)
```

**Arguments**

<code>h</code>	positive parameter
<code>alpha</code>	initial probabilities
<code>S</code>	sub-intensity
<code>beta</code>	parameter of transformation
<code>obs</code>	the observations
<code>weight</code>	weight of the observations
<code>rcens</code>	censored observations
<code>rcweight</code>	weight of the censored observations
<code>scale1</code>	scale for observations
<code>scale2</code>	scale for censored observations

---

logLikelihoodMpareto\_PADE

*Loglikelihood of matrix-Pareto using Pade*

---

### Description

Loglikelihood for a sample

### Usage

```
logLikelihoodMpareto_PADE(h, alpha, S, beta, obs, weight, rcens, rcweight)
```

### Arguments

h	nuisance parameter
alpha	initial probabilities
S	sub-intensity
beta	in-homogeneity parameter
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

logLikelihoodMpareto\_PADEs

*Loglikelihood of matrix-Pareto using Pade*

---

### Description

Loglikelihood for a sample

### Usage

```
logLikelihoodMpareto_PADEs(
  h,
  alpha,
  S,
  beta,
  obs,
  weight,
  rcens,
  rcweight,
  scale1,
  scale2
)
```

**Arguments**

h	nuisance parameter
alpha	initial probabilities
S	sub-intensity
beta	in-homogeneity parameter
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations
scale1	scale for observations
scale2	scale for censored observations

---

logLikelihoodMpareto\_RK

*Loglikelihood of matrix Pareto using RK*

---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMpareto_RK(h, alpha, S, beta, obs, weight, rcens, rcweight)
```

**Arguments**

h	step-length
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations



---

`logLikelihoodMpareto_RKs`*Loglikelihood of matrix-Pareto using RK*

---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMpareto_RKs(  
  h,  
  alpha,  
  S,  
  beta,  
  obs,  
  weight,  
  rcens,  
  rcweight,  
  scale1,  
  scale2  
)
```

**Arguments**

<code>h</code>	positive parameter
<code>alpha</code>	initial probabilities
<code>S</code>	sub-intensity
<code>beta</code>	parameter of transformation
<code>obs</code>	the observations
<code>weight</code>	weight of the observations
<code>rcens</code>	censored observations
<code>rcweight</code>	weight of the censored observations
<code>scale1</code>	scale for observations
<code>scale2</code>	scale for censored observations

---

logLikelihoodMpareto\_UNI

*Loglikelihood of matrix-Pareto using Uniformization*

---

### Description

Loglikelihood for a sample

### Usage

```
logLikelihoodMpareto_UNI(h, alpha, S, beta, obs, weight, rcens, rcweight)
```

### Arguments

h	positive parameter
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

logLikelihoodMpareto\_UNIs

*Loglikelihood of matrix-Pareto using Uniformization*

---

### Description

Loglikelihood for a sample

### Usage

```
logLikelihoodMpareto_UNIs(
  h,
  alpha,
  S,
  beta,
  obs,
  weight,
  rcens,
  rcweight,
  scale1,
  scale2
)
```

**Arguments**

h	positive parameter
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations
scale1	scale for observations
scale2	scale for censored observations

---

logLikelihoodMweibull\_PADE

*Loglikelihood of matrix-Weibull using Pade*


---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMweibull_PADE(h, alpha, S, beta, obs, weight, rcens, rcweight)
```

**Arguments**

h	nuisance parameter
alpha	initial probabilities
S	sub-intensity
beta	in-homogeneity parameter
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

logLikelihoodMweibull\_PADEs

*Loglikelihood of matrix-Weibull using Pade*

---

### **Description**

Loglikelihood for a sample

### **Usage**

```
logLikelihoodMweibull_PADEs(  
  h,  
  alpha,  
  S,  
  beta,  
  obs,  
  weight,  
  rcens,  
  rcweight,  
  scale1,  
  scale2  
)
```

### **Arguments**

h	nuisance parameter
alpha	initial probabilities
S	sub-intensity
beta	in-homogeneity parameter
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations
scale1	scale for observations
scale2	scale for censored observations

---

 logLikelihoodMweibull\_RK

*Loglikelihood of matrix Weibull using RK*


---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMweibull_RK(h, alpha, S, beta, obs, weight, rcens, rcweight)
```

**Arguments**

h	step-length
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

logLikelihoodMweibull\_RKs

*Loglikelihood of matrix-Weibull using RK*


---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMweibull_RKs(
  h,
  alpha,
  S,
  beta,
  obs,
  weight,
  rcens,
  rcweight,
  scale1,
  scale2
)
```

**Arguments**

h	positive parameter
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations
scale1	scale for observations
scale2	scale for censored observations

---

logLikelihoodMweibull\_UNI

*Loglikelihood of matrix-Weibull using Uniformization*

---

**Description**

Loglikelihood for a sample

**Usage**

logLikelihoodMweibull\_UNI(h, alpha, S, beta, obs, weight, rcens, rcweight)

**Arguments**

h	positive parameter
alpha	initial probabilities
S	sub-intensity
beta	parameter of transformation
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

`logLikelihoodMweibull_UNIs`*Loglikelihood of matrix-Weibull using Uniformization*

---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodMweibull_UNIs(  
  h,  
  alpha,  
  S,  
  beta,  
  obs,  
  weight,  
  rcens,  
  rcweight,  
  scale1,  
  scale2  
)
```

**Arguments**

<code>h</code>	positive parameter
<code>alpha</code>	initial probabilities
<code>S</code>	sub-intensity
<code>beta</code>	parameter of transformation
<code>obs</code>	the observations
<code>weight</code>	weight of the observations
<code>rcens</code>	censored observations
<code>rcweight</code>	weight of the censored observations
<code>scale1</code>	scale for observations
<code>scale2</code>	scale for censored observations

---

logLikelihoodPH\_PADE *Loglikelihood of PH using Pade*

---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodPH_PADE(h, alpha, S, obs, weight, rcens, rcweight)
```

**Arguments**

h	nuisance parameter
alpha	initial probabilities
S	sub-intensity
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

logLikelihoodPH\_PADEs *Loglikelihood of PH using Pade*

---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodPH_PADEs(
  h,
  alpha,
  S,
  obs,
  weight,
  rcens,
  rcweight,
  scale1,
  scale2
)
```



**Arguments**

h	nuisance parameter
alpha	initial probabilities
S	sub-intensity
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations
scale1	scale for observations
scale2	scale for censored observations

---

logLikelihoodPH\_RK     *Loglikelihood using RK*

---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodPH_RK(h, alpha, S, obs, weight, rcens, rcweight)
```

**Arguments**

h	step-length
alpha	initial probabilities
S	sub-intensity
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

logLikelihoodPH\_RKs    *Loglikelihood of PH using RK*

---

**Description**

Loglikelihood for a sample

**Usage**

logLikelihoodPH\_RKs(h, alpha, S, obs, weight, rcens, rcweight, scale1, scale2)

**Arguments**

h	positive parameter
alpha	initial probabilities
S	sub-intensity
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations
scale1	scale for observations
scale2	scale for censored observations

---

logLikelihoodPH\_UNI    *Loglikelihood using Uniformization*

---

**Description**

Loglikelihood for a sample

**Usage**

logLikelihoodPH\_UNI(h, alpha, S, obs, weight, rcens, rcweight)

**Arguments**

h	positive parameter
alpha	initial probabilities
S	sub-intensity
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations

---

logLikelihoodPH\_UNIs *Loglikelihood of PH using Uniformization*

---

**Description**

Loglikelihood for a sample

**Usage**

```
logLikelihoodPH_UNIs(h, alpha, S, obs, weight, rcens, rcweight, scale1, scale2)
```

**Arguments**

h	positive parameter
alpha	initial probabilities
S	sub-intensity
obs	the observations
weight	weight of the observations
rcens	censored observations
rcweight	weight of the censored observations
scale1	scale for observations
scale2	scale for censored observations

---

LRT *New Generic for doing a likelihood ratio test between two Matrix Distribution models*

---

**Description**

Methods are available for objects of class [ph](#)

**Usage**

```
LRT(x, y, ...)
```

**Arguments**

x, y	objects of the model class.
...	further parameters to be passed on

**Value**

a likelihood ratio test result.

---

LRT, ph, ph-method      *LRT Method for ph Class*

---

### Description

LRT Method for ph Class

### Usage

```
## S4 method for signature 'ph,ph'
LRT(x, y)
```

### Arguments

x, y                      objects of class [ph](#).

### Value

LRT between the models.

---

matrixExpSum\_arma      *Computes  $e^{(Sx)}$  base on the values on powerVector*

---

### Description

Computes  $e^{(Sx)}$  base on the values on powerVector

### Usage

```
matrixExpSum_arma(x, n, powerVector, a)
```

### Arguments

x	a number
n	an integer
powerVector	a vector
a	a number

---

matrixMax	<i>Maximum entry in a matrix</i>
-----------	----------------------------------

---

**Description**

Find the maximum entry

**Usage**

```
matrixMax(A)
```

**Arguments**

A                    a matrix

---

matrixMaxDiagonal	<i>Maximum entry in the diagonal of a matrix</i>
-------------------	--

---

**Description**

Maximum entry in the diagonal of a matrix

**Usage**

```
matrixMaxDiagonal(A)
```

**Arguments**

A                    a matrix

---

matrix_exponential	<i>Matrix exponential algorithm</i>
--------------------	-------------------------------------

---

**Description**

MATLAB's built-in algorithm - Pade approximation

**Usage**

```
matrix_exponential(Ainput)
```

**Arguments**

Ainput              a matrix

matrix\_exponential\_slow

*Matrix exponential algorithm*

---

**Description**

MATLAB's built-in algorithm - Pade approximation

**Usage**

matrix\_exponential\_slow(A)

**Arguments**

A                    a matrix

---

matrix\_inverse

*Inverse of a matrix*

---

**Description**

Computes the inverse

**Usage**

matrix\_inverse(A)

**Arguments**

A                    a matrix

---

matrix\_inverse\_slow

*Inverse of a matrix*

---

**Description**

Computes the inverse

**Usage**

matrix\_inverse\_slow(A)

**Arguments**

A                    a matrix

---

matrix_power	<i>Computes <math>A^n</math></i>
--------------	----------------------------------

---

**Description**

Computes  $A^n$

**Usage**

```
matrix_power(n, A)
```

**Arguments**

n	integer
A	a matrix

---

matrix_product	<i>Product of two matrices</i>
----------------	--------------------------------

---

**Description**

Product of two matrices

**Usage**

```
matrix_product(A1, A2)
```

**Arguments**

A1	matrix
A2	matrix

**Value**

Computes  $C = A1 * A2$

---

matrix\_product\_slow     *Product of two matrices*

---

**Description**

Product of two matrices

**Usage**

matrix\_product\_slow(a, b)

**Arguments**

a                    matrix

b                    matrix

**Value**

Computes  $c = a * b$

---

matrix\_sum             *Add matrices*

---

**Description**

Computes  $C = A + B$

**Usage**

matrix\_sum(A, B)

**Arguments**

A                    A matrix

B                    A matrix



---

matrix\_VanLoan      *Creates the matrix (A1, B1 ; 0, A2)*

---

**Description**

Creates the matrix (A1, B1 ; 0, A2)

**Usage**

matrix\_VanLoan(A1, A2, B1)

**Arguments**

A1	a matrix
A2	a matrix
B1	a matrix

---

matrix\_VanLoanArma      *Creates the matrix (A1, B1 ; 0, A2)*

---

**Description**

Creates the matrix (A1, B1 ; 0, A2)

**Usage**

matrix\_VanLoanArma(A1, A2, B1)

**Arguments**

A1	matrix
A2	matrix
B1	matrix

**Value**

Computes (A1, B1 ; 0, A2)

---

 maximum

*New Generic for Maximum of two Matrix Distributions*


---

**Description**

Methods are available for objects of class [ph](#)

**Usage**

```
maximum(x1, x2, ...)
```

**Arguments**

x1	an object of the model class.
x2	an object of the model class.
...	further parameters to be passed on

**Value**

A realization from the matrix distribution.

---

 maximum,iph,iph-method

*Maximum Method for inhomogeneous phase type distributions*


---

**Description**

Maximum Method for inhomogeneous phase type distributions

**Usage**

```
## S4 method for signature 'iph,iph'
maximum(x1, x2)
```

**Arguments**

x1	an object of class <a href="#">iph</a> .
x2	an object of class <a href="#">iph</a> .

**Value**

An object of class [iph](#).

**Examples**

```
iph1 <- iph(ph(structure = "general", dimension = 3), gfun = "weibull", gfun_pars = 2)
iph2 <- iph(ph(structure = "gcoxian", dimension = 5), gfun = "weibull", gfun_pars = 2)
iph_min <- maximum(iph1, iph2)
iph_min
```

---

maximum,ph,ph-method    *Maximum Method for phase type distributions*

---

**Description**

Maximum Method for phase type distributions

**Usage**

```
## S4 method for signature 'ph,ph'
maximum(x1, x2)
```

**Arguments**

x1                    an object of class [ph](#).  
x2                    an object of class [ph](#).

**Value**

An object of class [ph](#).

**Examples**

```
ph1 <- ph(structure = "general", dimension = 3)
ph2 <- ph(structure = "gcoxian", dimension = 5)
ph_min <- minimum(ph1, ph2)
ph_min
```

---

mgevcdf                    *Matrix GEV cdf*

---

**Description**

Computes the cdf (tail) of a matrix GEV distribution with parameters alpha, S and beta at x

**Usage**

```
mgevcdf(x, alpha, S, mu, sigma, xi, lower_tail = TRUE)
```

**Arguments**

x	non-negative value
alpha	Initial probabilities
S	sub-intensity matrix
mu	location parameter
sigma	scale parameter
xi	shape parameter
lower_tail	cdf or tail

**Value**

The cdf (tail) at x

---

mgevden

*Matrix GEV density*

---

**Description**

Computes the density of a matrix GEV distribution with parameters alpha, S and beta at x Dont allow for atoms in zero

**Usage**

mgevden(x, alpha, S, mu, sigma, xi)

**Arguments**

x	non-negative value
alpha	Initial probabilities
S	sub-intensity matrix
mu	location parameter
sigma	scale parameter
xi	shape parameter

**Value**

The density at x

---

mgompertzcdf	<i>Matrix Gompertz cdf</i>
--------------	----------------------------

---

**Description**

Computes the cdf (tail) of a matrix Gompertz distribution with parameters alpha, S and beta at x

**Usage**

```
mgompertzcdf(x, alpha, S, beta, lower_tail = TRUE)
```

**Arguments**

x	non-negative value
alpha	Initial probabilities
S	sub-intensity matrix
beta	shape parameter
lower_tail	cdf or tail

**Value**

The cdf (tail) at x

---

mgompertzden	<i>Matrix Gompertz density</i>
--------------	--------------------------------

---

**Description**

Computes the density of a matrix Gompertz distribution with parameters alpha, S and beta at x

**Usage**

```
mgompertzden(x, alpha, S, beta)
```

**Arguments**

x	non-negative value
alpha	Initial probabilities
S	sub-intensity matrix
beta	parameter

**Value**

The density at x

---

 minimum

*New Generic for Minimum of two Matrix Distributions*


---

**Description**

Methods are available for objects of class [ph](#)

**Usage**

```
minimum(x1, x2, ...)
```

**Arguments**

x1	an object of the model class.
x2	an object of the model class.
...	further parameters to be passed on

**Value**

A realization from the matrix distribution.

---

 minimum,iph,iph-method

*Minimum Method for inhomogeneous phase type distributions*


---

**Description**

Minimum Method for inhomogeneous phase type distributions

**Usage**

```
## S4 method for signature 'iph,iph'
minimum(x1, x2)
```

**Arguments**

x1	an object of class <a href="#">iph</a> .
x2	an object of class <a href="#">iph</a> .

**Value**

An object of class [iph](#).

**Examples**

```
iph1 <- iph(ph(structure = "general", dimension = 3), gfun = "weibull", gfun_pars = 2)
iph2 <- iph(ph(structure = "gcoxian", dimension = 5), gfun = "weibull", gfun_pars = 2)
iph_min <- minimum(iph1, iph2)
iph_min
```

---

minimum,ph,ph-method    *Minimum Method for phase type distributions*

---

**Description**

Minimum Method for phase type distributions

**Usage**

```
## S4 method for signature 'ph,ph'
minimum(x1, x2)
```

**Arguments**

x1                    an object of class [ph](#).  
x2                    an object of class [ph](#).

**Value**

An object of class [ph](#).

**Examples**

```
ph1 <- ph(structure = "general", dimension = 3)
ph2 <- ph(structure = "gcoxian", dimension = 5)
ph_min <- minimum(ph1, ph2)
ph_min
```

---

mloglogisticcdf            *Matrix Log-Logistic cdf*

---

**Description**

Computes the cdf (tail) of a matrix Log-Logistic distribution with parameters alpha, S and beta at x

**Usage**

```
mloglogisticcdf(x, alpha, S, beta, lower_tail = TRUE)
```

**Arguments**

x	non-negative value
alpha	Initial probabilities
S	sub-intensity matrix
beta	shape parameter
lower_tail	cdf or tail

**Value**

The cdf (tail) at x

---

<i>mloglogisticden</i>	<i>Matrix Log-Logistic density</i>
------------------------	------------------------------------

---

**Description**

Computes the density of a matrix Log-Logistic distribution with parameters alpha, S and beta at x

**Usage**

```
mloglogisticden(x, alpha, S, beta)
```

**Arguments**

x	non-negative value
alpha	Initial probabilities
S	sub-intensity matrix
beta	scale parameter

**Value**

The density at x



---

mlognormalcdf	<i>Matrix LogNormal cdf</i>
---------------	-----------------------------

---

**Description**

Computes the cdf (tail) of a matrix LogNormal distribution with parameters alpha, S and beta at x

**Usage**

```
mlognormalcdf(x, alpha, S, beta, lower_tail = TRUE)
```

**Arguments**

x	non-negative value
alpha	Initial probabilities
S	sub-intensity matrix
beta	shape parameter
lower_tail	cdf or tail

**Value**

The cdf (tail) at x

---

mlognormalden	<i>Matrix LogNormal density</i>
---------------	---------------------------------

---

**Description**

Computes the density of a matrix LogNormal distribution with parameters alpha, S and beta at x

**Usage**

```
mlognormalden(x, alpha, S, beta)
```

**Arguments**

x	non-negative value
alpha	Initial probabilities
S	sub-intensity matrix
beta	shape parameter

**Value**

The density at x

---

moment	<i>New Generic for Moment of Matrix Distributions</i>
--------	---

---

**Description**

Methods are available for objects of class `ph`

**Usage**

```
moment(x, ...)
```

**Arguments**

x	an object of the model class.
...	further parameters to be passed on

**Value**

A realization from the matrix distribution.

---

moment,ph-method	<i>Moment Method for phase type distributions</i>
------------------	---

---

**Description**

Moment Method for phase type distributions

**Usage**

```
## S4 method for signature 'ph'
moment(x, k = 1)
```

**Arguments**

x	an object of class <code>ph</code> .
k	a positive integer (moment order).

**Value**

The raw moment of the `ph` (or underlying `ph`) object.

**Examples**

```
set.seed(123)
ph1 <- ph(structure = "general", dimension = 3)
moment(ph1, 2)
```

---

mparetocdf	<i>Matrix Pareto cdf</i>
------------	--------------------------

---

**Description**

Computes the cdf (tail) of a matrix Pareto distribution with parameters alpha, S and beta at x

**Usage**

```
mparetocdf(x, alpha, S, beta, lower_tail = TRUE)
```

**Arguments**

x	non-negative value
alpha	Initial probabilities
S	sub-intensity matrix
beta	shape parameter
lower_tail	cdf or tail

**Value**

The cdf (tail) at x

---

mparetoden	<i>Matrix Pareto density</i>
------------	------------------------------

---

**Description**

Computes the density of a matrix Pareto distribution with parameters alpha, S and beta at x

**Usage**

```
mparetoden(x, alpha, S, beta)
```

**Arguments**

x	non-negative value
alpha	Initial probabilities
S	sub-intensity matrix
beta	scale parameter

**Value**

The density at x

---

mweibullcdf	<i>Matrix Weibull cdf</i>
-------------	---------------------------

---

**Description**

Computes the cdf (tail) of a matrix Weibull distribution with parameters alpha, S and beta at x

**Usage**

```
mweibullcdf(x, alpha, S, beta, lower_tail)
```

**Arguments**

x	non-negative value
alpha	Initial probabilities
S	sub-intensity matrix
beta	shape parameter
lower_tail	cdf or tail

**Value**

The cdf (tail) at x

---

mweibullden	<i>Matrix Weibull density</i>
-------------	-------------------------------

---

**Description**

Computes the density of a matrix Weibull distribution with parameters alpha, S and beta at x

**Usage**

```
mweibullden(x, alpha, S, beta)
```

**Arguments**

x	non-negative value
alpha	Initial probabilities
S	sub-intensity matrix
beta	shape parameter

**Value**

The density at x

---

newState	<i>New state in a Markov jump process</i>
----------	---

---

**Description**

Given a transition matrix Q, a uniform value u, and a previous state k, it returns the new state of a Markov jump process

**Usage**

```
newState(previousState, cumulatedEmbeddedMC, u)
```

**Arguments**

previousState	Previous state of the Markov jump process
cumulatedEmbeddedMC	A transition matrix
u	A random value in (0,1)

**Value**

The next state of the Markov jump process

---

ph	<i>Constructor Function for phase type distributions</i>
----	--

---

**Description**

Constructor Function for phase type distributions

**Usage**

```
ph(alpha = NULL, S = NULL, structure = NULL, dimension = 3)
```

**Arguments**

alpha	a probability vector.
S	a sub-intensity matrix.
structure	a valid ph structure ("general", "coxian", "hyperexponential", "gcoxian", "gerlang").
dimension	the dimension of the ph structure (if structure is provided).

**Value**

An object of class [ph](#).

**Examples**

```
ph(structure = "gcoxian", dim = 5)
ph(alpha = c(.5, .5), S = matrix(c(-1, .5, .5, -1), 2, 2))
```

---

ph-class	<i>Phase Type distributions</i>
----------	---------------------------------

---

**Description**

Class of objects for phase type distributions

**Value**

Class object

**Slots**

name name of the phase type distribution.  
 pars a list comprising of the parameters.  
 fit a list containing estimation information.

---

phcdf	<i>Phase-type cdf or tail</i>
-------	-------------------------------

---

**Description**

Computes the cdf of phase-type distribution with parameters alpha and S at x

**Usage**

```
phcdf(x, alpha, S, lower_tail = TRUE)
```

**Arguments**

x	non-negative value
alpha	Initial probabilities
S	sub-intensity matrix
lower_tail	cdf or tail

**Value**

The cdf (tail) at x

---

phdensity	<i>Phase-type density</i>
-----------	---------------------------

---

**Description**

Computes the density of phase-type distribution with parameters alpha and S at x

**Usage**

```
phdensity(x, alpha, S)
```

**Arguments**

x	non-negative value
alpha	Initial probabilities
S	sub-intensity matrix

**Value**

The density at x

---

quan	<i>New Generic for the Quantile of Matrix Distributions</i>
------	---

---

**Description**

Methods are available for objects of class [ph](#)

**Usage**

```
quan(x, ...)
```

**Arguments**

x	an object of the model class.
...	further parameters to be passed on

**Value**

Quantile from the matrix distribution.

---

quan, ph-method      *Quantile Method for phase type distributions*

---

### Description

Quantile Method for phase type distributions

### Usage

```
## S4 method for signature 'ph'
quan(x, p)
```

### Arguments

x                    an object of class `ph`.  
p                    a vector of probabilities.

### Value

A list containing the probabilities and corresponding quantile evaluations.

### Examples

```
obj <- ph(structure = "general")
quan(obj, c(0.5, 0.9, 0.99))
```

---

random\_structure      *Random structure of a phase-type*

---

### Description

Generates random parameters  $\alpha$  and  $S$  of a phase-type distribution of dimension  $p$  with chosen structure

### Usage

```
random_structure(p, structure = "general", scale_factor = 1)
```

### Arguments

p                    Dimension of the phase-type  
structure          Type of structure: "general", "hyperexponential", "gerlang", "coxian" or "gcoxian"  
scale\_factor      A factor that multiplies the sub-intensity matrix

### Value

Random parameters  $\alpha$  and  $S$  of a phase-type



---

reg	<i>New Generic for Regression with Matrix Distributions</i>
-----	---

---

**Description**

Methods are available for objects of class [ph](#)

**Usage**

```
reg(x, y, ...)
```

**Arguments**

x	an object of the model class.
y	a vector of data.
...	further parameters to be passed on

**Value**

An object of the fitted model class.

---

reg,ph-method	<i>Regression Method for ph Class</i>
---------------	---------------------------------------

---

**Description**

Regression Method for ph Class

**Usage**

```
## S4 method for signature 'ph'
reg(
  x,
  y,
  weight = numeric(),
  rcen = numeric(),
  rcenweight = numeric(),
  X = numeric(),
  B0 = numeric(),
  stepsEM = 1000,
  methods = c("RK", "UNI"),
  rkstep = NA,
  uni_epsilon = NA,
  optim_method = "BFGS",
  maxit = 50,
```

```

    reltol = 1e-08,
    every = 10
)

```

### Arguments

x	an object of class <a href="#">ph</a> .
y	vector or data.
weight	vector of weights.
rcen	vector of right-censored observations
rcenweight	vector of weights for right-censored observations.
X	model matrix (no intercept needed).
B0	initial regression coefficients (optional).
stepsEM	number of EM steps to be performed.
methods	methods to use for matrix exponential calculation: RM, UNI or PADE
rkstep	Runge-Kutta step size (optional)
uni_epsilon	epsilon parameter for uniformization method
optim_method	method to use in gradient optimization
maxit	maximum number of iterations when optimizing g function.
reltol	relative tolerance when optimizing g function.
every	number of iterations between likelihood display updates.

### Value

An object of class [sph](#).

---

reversTransformData	<i>Applies the inverse of the GEV but giving back the vector in reverse order</i>
---------------------	---

---

### Description

Used for EM step

### Usage

```
reversTransformData(observations, weights, beta)
```

### Arguments

observations	the observations
weights	weithgs of the observations
beta	parameters of the GEV

---

riph	<i>Random inhomogeneous phase-type</i>
------	--

---

**Description**

Generates a sample of size  $n$  from an inhomogeneous phase-type distribution with parameters  $\alpha$ ,  $S$  and  $\beta$

**Usage**

```
riph(n, dist_type, alpha, S, beta)
```

**Arguments**

$n$	Sample size
$dist\_type$	Type of IPH
$\alpha$	Initial probabilities
$S$	sub-intensity matrix
$\beta$	Parameter of the transformation

**Value**

The simulated sample

---

rmatrixgev	<i>Random matrix GEV</i>
------------	--------------------------

---

**Description**

Generates a sample of size  $n$  from an inhomogeneous phase-type distribution with parameters  $\alpha$ ,  $S$  and  $\beta$

**Usage**

```
rmatrixgev(n, alpha, S, mu, sigma, xi = 0)
```

**Arguments**

$n$	Sample size
$\alpha$	Initial probabilities
$S$	sub-intensity matrix
$\mu$	Location parameter
$\sigma$	Scale parameter
$\xi$	Shape parameter: Default 0 which corresponds to the Gumbel case

**Value**

The simulated sample

---

rphasetype	<i>Random phase-type</i>
------------	--------------------------

---

**Description**

Generates a sample of size  $n$  from a phase-type distribution with parameters  $\alpha$  and  $S$

**Usage**

rphasetype( $n$ ,  $\alpha$ ,  $S$ )

**Arguments**

$n$	Sample size
$\alpha$	Initial probabilities
$S$	sub-intensity matrix

**Value**

The simulated sample

---

runge_kutta	<i>Runge Kutta for the calculation of the a,b and c vectors in a EM step</i>
-------------	--

---

**Description**

Performce the RK of forth order

**Usage**

runge\_kutta(avector, bvector, cmatrix, dt, h, S, t)

**Arguments**

avector	the a vector
bvector	the b vector
cmatrix	the c matrix
dt	the increment
h	step-length
S	sub-intensity
t	exit rates

---

show, iph-method	<i>Show Method for inhomogeneous phase type distributions</i>
------------------	---

---

**Description**

Show Method for inhomogeneous phase type distributions

**Usage**

```
## S4 method for signature 'iph'  
show(object)
```

**Arguments**

object            an object of class [iph](#).

---

show, ph-method	<i>Show Method for phase type distributions</i>
-----------------	---

---

**Description**

Show Method for phase type distributions

**Usage**

```
## S4 method for signature 'ph'  
show(object)
```

**Arguments**

object            an object of class [ph](#).

---

show, sph-method	<i>Show Method for survival phase type objects</i>
------------------	--

---

**Description**

Show Method for survival phase type objects

**Usage**

```
## S4 method for signature 'sph'  
show(object)
```

**Arguments**

object            an object of class [sph](#).

---

sim	<i>New Generic for Simulating Matrix Distributions</i>
-----	--

---

**Description**

Methods are available for objects of class `ph`

**Usage**

```
sim(x, ...)
```

**Arguments**

x	an object of the model class.
...	further parameters to be passed on

**Value**

A realization from the matrix distribution.

---

sim,iph-method	<i>Simulation Method for inhomogeneous phase type distributions</i>
----------------	---

---

**Description**

Simulation Method for inhomogeneous phase type distributions

**Usage**

```
## S4 method for signature 'iph'
sim(x, n = 1000)
```

**Arguments**

x	an object of class <code>iph</code> .
n	an integer of length of realization.

**Value**

A realization of independent and identically distributed inhomogeneous phase-type variables.

**Examples**

```
obj <- iph(ph(structure = "general"), gfun = "lognormal", gfun_pars = 2)
sim(obj, n = 100)
```

---

sim,ph-method	<i>Simulation Method for phase type distributions</i>
---------------	---

---

**Description**

Simulation Method for phase type distributions

**Usage**

```
## S4 method for signature 'ph'  
sim(x, n = 1000)
```

**Arguments**

x	an object of class <a href="#">ph</a> .
n	an integer of length of realization.

**Value**

A realization of independent and identically distributed phase-type variables.

**Examples**

```
obj <- ph(structure = "general")  
sim(obj, n = 100)
```

---

solve_linear_system	<i>Solves a system with multiple right hand sides</i>
---------------------	---

---

**Description**

$AX=B$  which can be decomposed as  $LUX=B$  and finds  $X$ . When  $B$  is the identity matrix the solution is the inverse of  $A$

**Usage**

```
solve_linear_system(A1, B)
```

**Arguments**

A1	a matrix
B	a matrix

---

sph

*Constructor Function for Survival phase type objects*

---

**Description**

Constructor Function for Survival phase type objects

**Usage**

```
sph(x = NULL, coefs = list(B = numeric(0), C = numeric(0)), type = "reg")
```

**Arguments**

x	An object of class <a href="#">ph</a>
coefs	coefficients of the survival regression object.
type	type of survival object.

**Value**

An object of class [sph](#).

---

sph-class

*Survival Analysis for Phase Type distributions*

---

**Description**

Class of objects for inhomogeneous phase type distributions

**Value**

Class object

**Slots**

coefs coefficients of the survival regression object.  
type type of survival object.



---

sumPH                      *Computes the initial distribution and sub-intensity of the sum of PH*

---

**Description**

Computes the initial distribution and sub-intensity of the sum of PH

**Usage**

sumPH(alpha1, S1, alpha2, S2)

**Arguments**

alpha1	initial distribution
S1	sub-intensity
alpha2	initial distribution
S2	sub-intensity

---

vectorOfMatrices\_arma    *Computes elements  $S^n / n!$  until the value size*

---

**Description**

Computes elements  $S^n / n!$  until the value size

**Usage**

vectorOfMatrices\_arma(theVector, S, a, sizevect)

**Arguments**

theVector	a vector
S	sub-untensity matrix
a	a number
sizevect	size of vector

---

`vectorOfMatrices_arma2`*Computes elements  $S^n / n!$  until the value size*

---

**Description**

Computes elements  $S^n / n!$  until the value size

**Usage**

```
vectorOfMatrices_arma2(theVector, S, sizevect)
```

**Arguments**

<code>theVector</code>	a vector
<code>S</code>	sub-unity matrix
<code>sizevect</code>	size of vector

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